

# TOPNOST, HITROST RAZTAPLJANJA

**Definicija:** Topnost (oz. nasičena raztopina) predstavlja stanje, ko je topljenec (trdni, tekoči, plinast) v ravnotežju z raztopino (topljenecem, raztopljenim v topilu).

- kvantitativni izraz
- pri določeni T
- homogena molekularna disperzija

**Pojma:** nasičena raztopina, prenasičena (supersaturated) raztopina

**Fazno pravilo** – topnost (primeri: mešanje dveh tekočin, fenol, voda; evtektik – timol, salol)

**Načini izražanja topnosti:** US farmakopeja (tudi Ph. Jug. IV)

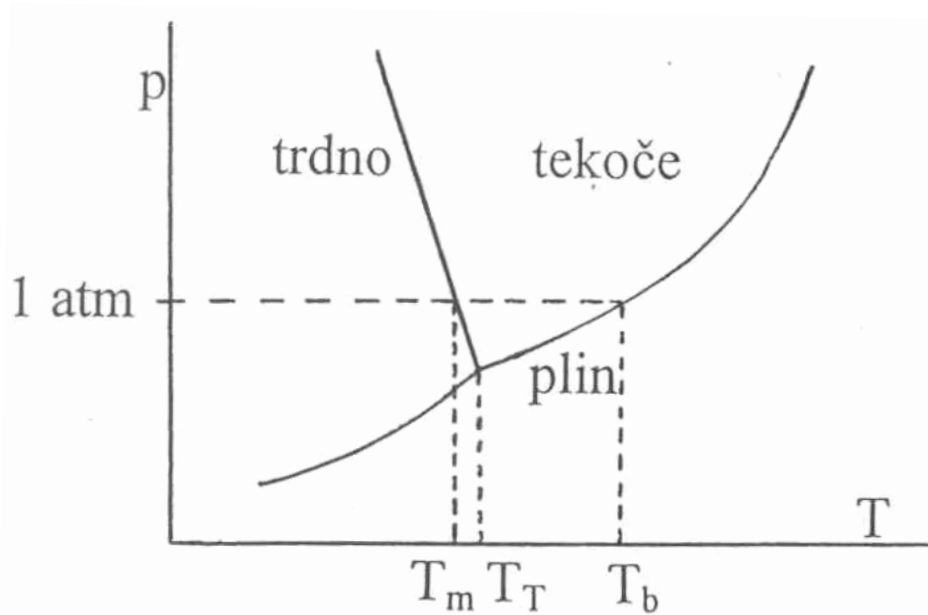
št. ml topila, v katerih se raztopi 1 g topljenca (npr. 1 g borne kisline se raztopi v 18 mL vode).

Molalnost, molarnost, procenti

**Interakcije topilo – topljenec:** “Podobno se topi v podobnem”; polarnost (dipolni moment) – ni vedno dovolj. Vodikova vez, kisl. – bazične lastnosti (Lewis) → interakcije; razmerje polarne : nepolarne skupine; razvejanje (n – butil alkohol – 8 g/100 mL H<sub>2</sub>O, terciarni butanol v vseh razmerjih topen s H<sub>2</sub>O). **Dielektrična konstanta:** 80 – H<sub>2</sub>O, 5 – CH<sub>3</sub>Cl, 2 – benzen.

**Acido – bazna ravnotežja:** šibke kisl. (organske narave) niso popolnoma topne v H<sub>2</sub>O; npr. fenoli in karboksilne kisline – dobro topne v raztopinah močnih baz.

**Solvatacija** – dipolne interakcije, npr. H – vez → ↑ topnost



**T<sub>m</sub>, T<sub>T</sub>**

# IDEALNA TOPNOST

V ravnotežju:

$$\mu_B(l) = \mu_B^*(s)$$

$$\mu_B(l) = \mu_B^*(l) + RT \ln x_B$$

$$\mu_B^*(s) = \mu_B^*(l) + RT \ln x_B$$

$$\ln x_B = \frac{\mu_B^*(s) - \mu_B^*(l)}{RT} = -\frac{\Delta G_{\text{fus}}}{RT} = -\frac{\Delta H_{\text{fus}}}{RT} + \frac{\Delta S_{\text{fus}}}{R}$$

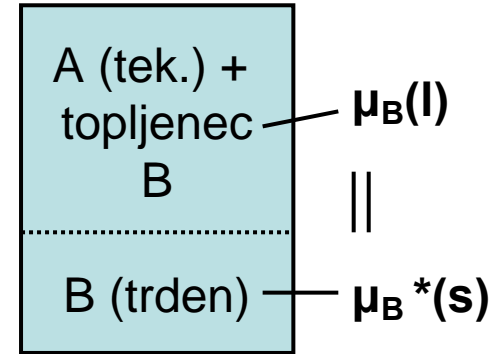
$\Delta S_{\text{fus}}$  in  $\Delta H_{\text{fus}} = \text{konst.}$  v širšem T območju

Pri  $T^*$  (temperatura tališča) je  $\Delta G_{\text{fus}} = 0 \rightarrow$

$$0 = -\frac{\Delta H_{\text{fus}}}{RT^*} + \frac{\Delta S_{\text{fus}}}{R}$$

in pri T: 
$$\ln x_B = \frac{-\Delta H_{\text{fus}}}{RT} + \frac{\Delta S_{\text{fus}}}{R}$$

$$\ln x_B = \frac{-\Delta H_{\text{fus}}}{R} \left( \frac{1}{T} - \frac{1}{T^*} \right)$$



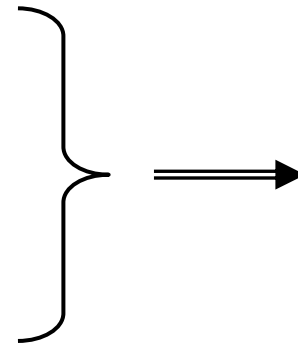
# IDEALNA TOPNOST

$$\left. \begin{aligned} \mu_B(\text{l}) &= \mu_B^*(\text{s}) \\ \mu_B(\text{l}) &= \mu_B^*(\text{l}) + RT \ln x_B \end{aligned} \right\} \mu_B^*(\text{s}) = \mu_B^*(\text{l}) + RT \ln x_B$$

$$\ln x_B = \frac{\mu_B^*(\text{s}) - \mu_B^*(\text{l})}{RT} = -\frac{\Delta G_{\text{fus}}}{RT} = -\frac{\Delta H_{\text{fus}}}{RT} + \frac{\Delta S_{\text{fus}}}{R}$$

$$T = T_{\text{tal}}(T^*) = 0 = -\frac{\Delta H_{\text{fus}}}{RT^*} + \frac{\Delta S_{\text{fus}}}{R}$$

$$T = \text{neka } T = \ln x_B = -\frac{\Delta H_{\text{fus}}}{RT} + \frac{\Delta S_{\text{fus}}}{R}$$

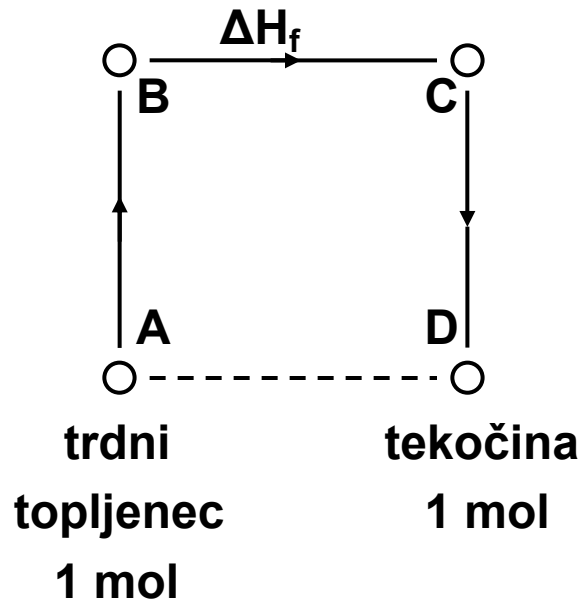


$$\ln x_B = -\frac{\Delta H_{\text{fus}}}{R} \left( \frac{1}{T} - \frac{1}{T^*} \right)$$

trojna točka topljenja  
temp.  $T_t$

$$\Delta H_{A-B} = \int_T^{T_t} c_{p,s} dT$$

$$\Delta S_{A-B} = \int_T^{T_t} (c_{p,s}/T) dT$$



$$\Delta H_{C-D} = \int_{T_t}^T c_{p,l} dT$$

$$\Delta S_{C-D} = \int_{T_t}^T (c_{p,l}/T) dT$$

temperatura določanja  
topnosti topljenja ( $T$ )

$$\Delta G_{A-D} = \mu_l - \mu_s = RT \ln(f_l/f_s)$$

$f_l = f_0 =$  fugativnost standardnega stanja

$$a = f/f_0 (P/P_0) = x\gamma$$

$$\Delta G = \mu_l - \mu_s = RT \ln(f_l/f_s)$$

Ker velja:  $\mu_i = \mu_i^0 + RT \ln(f_i/f_i^0)$

fazi  $\alpha, \beta$ :

$$\mu_i^\alpha = \mu_i^{0\alpha} + RT \ln(f_i^\alpha/f_i^{0\alpha})$$

$$\mu_i^\beta = \mu_i^{0\beta} + RT \ln(f_i^\beta/f_i^{0\beta})$$

fazi  $\alpha, \beta$  v ravnotežju:  $\mu_i^\alpha = \mu_i^\beta$

$$\mu_i^{0\alpha} + RT \ln(f_i^\alpha/f_i^{0\alpha}) = \mu_i^{0\beta} + RT \ln(f_i^\beta/f_i^{0\beta}) \quad (\text{X})$$

1. Če sta standardni stanji komponente  $i$  v obeh fazah enaki:

$$\mu_i^{0\alpha} = \mu_i^{0\beta} \Rightarrow f_i^{0\alpha} = f_i^{0\beta} \Rightarrow f_i^\alpha = f_i^\beta$$

2. Standardno stanje komponente  $i$  je v obeh fazah pri enaki temperaturi, vendar pa sta  $p$  in sestava obeh faz različna:

$$\mu_i^{0\alpha} = \mu_i^{0\beta} + RT \ln(f_i^{0\alpha}/f_i^{0\beta})$$

Če ta izraz vstavimo v enačbo X, spet dobimo:

$$f_i^\alpha = f_i^\beta$$

Ravnotežje, izraženo s kemijskimi potenciali, lahko nadomestimo z izrazom, da morajo biti fugativnosti pri dani T za katerokoli i komponento enake v vseh fazah.

Idealna topnost:  $\gamma = 1$

$$\Delta G_{A-D} = -RT \cdot \ln a = \underline{\underline{-RT \cdot \ln x}}$$

$$\Delta G_{A-D} = \Delta H_{A-D} - T\Delta S_{A-D}$$

$$\Delta H_{A-D} = \Delta H_{A-B} + \Delta H_{B-C} + \Delta H_{C-D}$$

$$\begin{aligned} \Delta H_{A-D} &= \int_T^{T_t} c_{p,s} dT + \Delta H_f + \int_{T_t}^T c_{p,l} dT = \Delta H_f + c_{p,s}(T_t - T) + c_{p,l}(T - T_t) = \\ &= \Delta H_f + (c_{p,s} - c_{p,l})(T_t - T) \end{aligned}$$

Če je:  $\Delta c_p = \Delta c_{p,l} - \Delta c_{p,s} \rightarrow$

$$\Delta H_{A-D} = \Delta H_f + \Delta c_p (T - T_t) = \Delta H_f + \int_{T_t}^T \Delta c_p dT$$

molska toplotna kapaciteta: pri  $p = \text{konst.}$ :  $c_p = (\delta H / \delta T)_p$

pri  $V = \text{konst.}$ :  $c_v = (\delta U / \delta T)_v$

$c_p > c_v$  (pri  $p = \text{konst.}$  se  $T$  dvigne manj – zaradi dela, ki ga sistem opravlja, kot pri  $V = \text{konst.}$ )

**Idealni plin:**  $c_p - c_v = \left( \frac{\delta H}{\delta T} \right)_p - \left( \frac{\delta U}{\delta T} \right)_p$  (pri  $p = \text{konst.}$ )

$H = U + pV = U + nRT \rightarrow$

$$c_p - c_v = \left( \frac{\delta U}{\delta T} \right)_p + nR - \left( \frac{\delta U}{\delta T} \right)_p = \underline{\underline{nR}}$$



$$\underline{\underline{\Delta S_{A-D} = \Delta S_f + \int_{T_t}^T (\Delta c_p / T) dT}}$$

pri  $T_t$ :  $\Delta S_f = \Delta H_f / T_t$

Kombinacija gornjih enačb (za  $\Delta G_{A-D}$ ,  $\Delta H_{A-D}$ ,  $\Delta S_{A-D}$ ):

$$\Delta G_{A-D} = \Delta H_{A-D} - T \Delta S_{A-D}$$

$$\Delta G_{A-D} = \Delta H_f + \int_{T_t}^T \Delta c_p dT - T \left( \frac{\Delta H_f}{T_t} + \Delta c_p \ln \frac{T}{T_t} \right)$$

$$\Delta G_{A-D} = -RT \cdot \ln x$$

$$\begin{aligned} \ln x &= -\frac{\Delta H_f}{RT} - \frac{\Delta c_p}{RT} (T - T_t) + \frac{T \Delta H_f}{RT \cdot T_t} + \frac{T \Delta c_p}{RT} \cdot \ln \frac{T}{T_t} = \\ &= -\frac{\Delta H_f}{RT_t} \left( \frac{T_t - T}{T} \right) + \frac{\Delta c_p (T_t - T)}{RT} - \frac{\Delta c_p}{R} \cdot \ln \frac{T_t}{T} \end{aligned}$$

Ker je  $T_t \approx T_m$  (temperatura tališča)

$\Delta c_p$  = majhna vrednost in

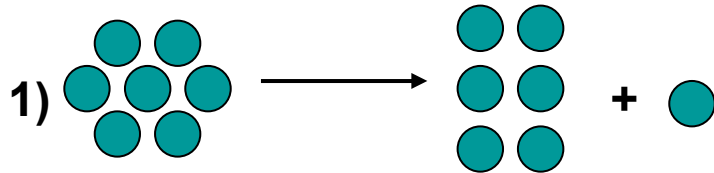
$$\frac{T_m - T}{T} \approx \ln \frac{T_m}{T} \quad (\text{Taylorjeva vrsta})$$

$$\left( \begin{array}{l} \ln \frac{T_m}{T} = \frac{T + \Delta T}{T} = \ln 1 + x \quad (x = \Delta T / T) \\ \frac{T_m - T}{T} = \frac{T + \Delta T - T}{T} = \frac{\Delta T}{T} \quad (= x) \end{array} \right)$$

$$\ln x = -\frac{\Delta H_f}{RT_m} \left( \frac{T_m - T}{T} \right) = \underline{\underline{-\frac{\Delta S_f}{R} \left( \frac{T_m - T}{T} \right)}}$$

$$\ln x = -\frac{\Delta S_f}{R} \left( \frac{T_m - T}{T} \right) - \ln \gamma$$

# DOLOČITEV AKTIVNOSTNEGA KOEFICIENTA ( $\gamma_2$ ) V ENAČBI ZA TOPNOST



topljenec

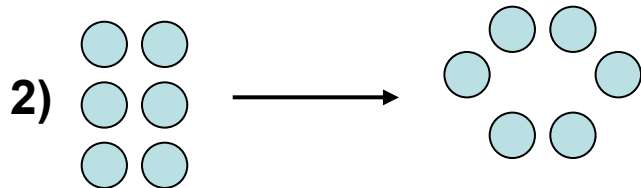
molekula topljenca se loči od faze topljenca in preide v parno fazo

Cepitev vezi med 2 sosednjima molekulama, delo:  $2 w_{22}$

22 – indeks, nanaša se na interakcije med molekulami topljenca

Prostor, ki nastane, molekule topljenca zaprejo:  $E = - w_{22}$  (se sprosti).

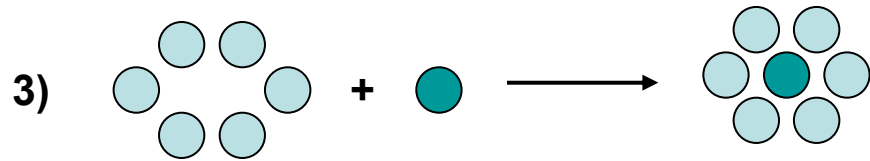
$\Sigma$ delo:  $w_{22}$



topilo

tvorba prostora v topilu

Delo za ta korak:  $w_{11}$  (indeks 11 – interakcije med molekulami topila)



molekula topljenca preide iz parne faze v nastali prostor

Pridobljeno delo (znižanje potencialne energije):  $-w_{12}$

Ko se zasedeni prostor zapre: potencialna energija se dodatno zniža za:

$$-w_{12} \cdot \Sigma \text{delo (energ.)} = -2w_{12}$$

**Celotno delo (energija)** za ta proces:  $w_{22} + w_{11} - 2w_{12}$

$$\ln \gamma_2 = (w_{22} + w_{11} - 2w_{12}) \frac{V_2 \Phi_1^2}{RT}$$

$V_2$  – molarni volumen (podhlajene) taline topljenca

$\Phi_1$  – volumski delež topila ( $x_1 V_1 / (x_1 V_1 + x_2 V_2)$ )